# MULTI-MODE REPRESENTATION OF MOTION DATA

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Abstract: We investigate the use of multi-linear models to represent human motion data. We show that naturally occur-

ring modes in several classes of motion can be used to efficiently represent the motions for various animation tasks, such as dimensionality reduction or synthesis of new motions by morphing. We show that especially for the approximations of motions by few components the reduction based on a multi-linear model can be

considerably better than one obtained by principal component analysis (PCA).

# 1 INTRODUCTION

The use and reuse of motion data recorded by motion capture systems is an important technique in computer animation. Usually the motion data are represented as sequences of poses, which in general employ skeletal representations of motion data. In the last few years also data bases of motions have been used to synthesize or analyze motions in various ways, see e.g. (Giese and Poggio, 2000; Troje, 2002; Kovar et al., 2002; Safonova et al., 2004; Kovar and Gleicher, 2004; Ormoneit et al., 2005; Majkowska et al., 2006).

Whereas the use of temporal alignments of motion in these data bases is well established (Bruderlin and Williams, 1995; Giese and Poggio, 2000; Kovar and Gleicher, 2003; Hsu et al., 2005) and the use of linear models for representing motions and their dimensionality reduction by principal component analysis (PCA) is also a well established technique in various contexts (Barbič et al., 2004; Chai and Hodgins, 2005; Safonova et al., 2004; Glardon et al., 2004; Troje, 2002; Ormoneit et al., 2005), little work has been done to employ the multi-linear structure of the motion data bases or to use the physics-based layer for the temporal alignment. Whereas some work has been done on using the physics-based layer (Majkowska et al., 2006; Safonova and Hodgins, 2005) as distance measures, the only work we are aware of on using multi-linear models for motion data is (Mukai

and Kuriyama, 2006).

The very successful use of multi-linear models in the context of facial animation (Vlasic et al., 2005) has been a major motivation for us to investigate them in the context of motion capture data.

## 1.1 Our Contribution

In the following we will show that using naturally occurring modes in several classes of motion can be used to efficiently represent the motions in a multi-linear model.

Using a data base of captured motions in which several actors performed various motions in different styles in different interpretations we build multi-mode representations of various classes of motions:

- For one class of motions the motions have to be time-aligned and warped.
  - Whereas in principal any time warping method could be used for this task, we found it beneficial to use distance measures involving the physics-based layer of a motion.
- A higher-order data tensor  $\Delta$  is built using different modes of the motions.
- Using an higher-order SVD a core tensor Φ can be computed, which can be used for representing low-dimensional approximations of the motions.

We investigate the properties of the resulting multi-mode representation, especially with respect to

dimensionality reduction and its suitability for synthesizing new motions by morphing.

We will show that especially for the approximations of motions by few components the reduction based on a multi-linear model can be considerably better than one obtained by principal component analysis (PCA).

# 2 MULTI-LINEAR ALGEBRA

For our tensor operations we use multi-linear algebra which is an generalization of linear algebra.

A tensor is the basic mathematical object of multilinear algebra, it is a generalization of vectors (tensor 1st order) and matrices (tensor 2nd order). A tensor of nth order can be thought as an n-dimensional block of data. While within a matrix the two dimensions (columns and rows) correspond to two modes, a tensor can be build up with more general modes. A more detailed description of multi-linear algebra is given in (Vlasic et al., 2005).

# 2.1 Tensor Construction

There are different natural possibilities to fill the data tensor  $\Delta$  of our multi-mode model. Some do not require any preprocessing, some require e.g. a temporal alignment of the motions. In the following we investigate the use of six different modes:

 a) Actor Mode, all motions are captured from different people.

In our example motion data base, the actors were given the same instructions how to perform the motions. The five actors performing the motions all have been healthy young adult male persons.

b) **Style Mode**, when possible we captured several styles of the motion classes.

The meaning of style differs for the various motion classes; we describe them more closely in section 4.

 Repetition Mode (Interpretation Mode), all motions are captured several times.

The instructors were told to stay within the same verbal description of the motion and its style, but nevertheless to have some variations in their interpretations of the motion and the style.

These are quite generally applicable modes, they consist of complete motions that span the space of the considered motion classes.

The following modes are of a more technical nature.

- d) **Data Mode**, all information of a motion is stacked into a single vector.
- e) **Frame Mode**, this mode space is spanned by the frames of the captured motions.
- f) DOF Mode, all motion degrees of freedom are separated in this mode. This mode depends on the representation of the motion data.

They give a description of how the motion data are arranged for the tensor construction. Either we stack a complete motion into the Data Mode or the motion is split into the Frame and DOF Mode. In (Mukai and Kuriyama, 2006) the authors only focus on joint, time and motion correlations, hence they are just using some technical modes.

#### 2.2 Data Tensor

A tensor with the smallest number of modes was created by using the natural modes a, b and c. Therefore the motion data have to be filled into one vector to construct the data mode. The matrix of size  $n \times f$ , which represents one motion, is stacked into one column. With this arrangement we obtain a tensor in the size of  $f \cdot n \times a \times b \times c$ , where a is the number of actors in the Personal Mode, b is the size of the different motion styles used for the Style Mode, c is the number of motion sequences in the Repetition Mode, f is the number of frames in the Frame Mode and n is the number of degrees of freedom for the given motion representation.

A further tensor of a higher order is constructed by using the three natural modes and the Frame and DOF Mode. The result is a data tensor  $\Delta$  which has a size of  $f \times n \times a \times b \times c$ .

#### 2.3 N-Mode SVD

Similar to (Vlasic et al., 2005), the data tensors  $\Delta_i$  can be transformed by an N-mode singular value decomposition (N-mode SVD). For this purpose we used the N-way Toolbox (C. A. Andersson and R. Bro, 2000). The result is a tensor  $\Phi_i'$  and respective matrices  $U_i$ . Mathematically this can be expressed in the following way:

$$\Delta_i = \Phi_i' \times_1 U_{i,1} \times_2 U_{i,2} \dots \times_n U_{i,n}$$

Where  $\times_n$  describes the mode-n product. Mode-n-multiplying a tensor T with matrix M replaces every mode-n-vector v of T with a transformed vector Mv.

A reduced model  $\Phi_i$  can be obtained by truncation of insignificant components from  $\Phi_i'$  and of matrices  $U_i$ , respectively. In the special case of a 2-mode tensor this procedure is equivalent to principal component analysis (PCA).

## 2.4 Motion Reconstruction

Once we have obtained the reduced model  $\Phi_i$  and its associated matrices  $U_i$ , we are able to approximate any original motion. This is done by first mode-multiplying the core tensor with every matrix  $U_i$  belonging to a technical mode, and then modemultiplying the resulting tensor with one row of every matrix belonging to a natural mode.

Furthermore, with this model in hand, we can generate an arbitrary interpolation of original motions by using linear combinations of rows of  $U_i$  with respect to the natural modes.

# 3 TIME WARPING

Dynamic time warping (DTW) algorithms are widely used in motion data processing to get a temporal correspondence of the used motions. Such a correspondence is needed to get reasonable realistic results when synthesizing motions (Bruderlin and Williams, 1995; Giese and Poggio, 2000; Kovar and Gleicher, 2003). The result of a time warp depends on the used algorithm, the given distance measurement and the features with which the motions are compared. Until now mainly kinematic features were used to compare whole body motions. Dynamic features were only used in the context of spliced body motions (Majkowska et al., 2006).

# 3.1 Iterative Multi-scale Dynamic Time Warping

We use the Iterative Multi-scale Dynamic Time Warping (IMDTW) algorithm presented by (Zinke and Mayer, 2006). This enhanced algorithm is used because it has no quadratic runtime and does not need quadratic memory space. This goal is reached by combining two approaches:

- The possible pathes are restricted
- The path is searched iteratively with several resolutions of the cost matrix

This iterative dynamic time warping algorithm works on windows of the given (maybe high dimensional) time series. After the first iteration we have got a path through the low resolution DTW matrix. We use a tube around this path for the next iteration where we calculate this tube with a smaller windows size what results in a higher resolution.

# 3.2 Distance Measure

Our time warping algorithm is parameterized with the following distance measure. For every frame i of a considered motion we build a frame feature vector f(i). This vector contains all properties of the motion that should be used for comparison. These frame feature vectors are put together over a frame window  $f(i), \ldots, f(i+n)$  as normalized sum to compute a feature vector  $\mathcal{F}(i)$ . Now we use the scalar product of these feature vectors to compute a distance between two motions:

$$D(\mathcal{F}_1(i), \mathcal{F}_2(j)) = 1 - \langle \mathcal{F}_1(i), \mathcal{F}_2(j) \rangle$$

By this method we can handle a lot of different features parallel. It is also possible to give a specific feature a special weight by scaling. This feature then contributes more to the direction the vector points in.

#### 3.3 Distance Features

We found it very beneficial to include features on the physics-based level. For this purpose the mass from all segments of a skeleton and their center of mass have to be calculated. We use the heuristics based on anthropometric tables described in (Robbins and Wu, 2003) for this purpose.

In addition to the center of mass (and its acceleration) of the entire body we also use the angular momentum of the body segments as physics-based features for comparing motions. Using a local coordinate system aligned to the motion, these features are independent of the starting position and orientation of the root segment. Although this local coordinate system strictly speaking is not an inertial system the occurring pseudo-forces are rather negligible for typical human motions.

All these simple features give a lot of information on the viewed motions. Based on the acceleration of the center of mass it is, for example, simple to detect non-contact phases. Then the COM-acceleration is equivalent to acceleration due to gravity when the body has no ground contact:

$$a_{\text{COM}} \approx a_{\text{earth}} = \begin{pmatrix} 0.0\\ -9.81\\ 0.0 \end{pmatrix}$$

Figure 1 shows the acceleration of the center of mass of a dancing motion. There are three non-contact phases that can be easily detected by analyzing the *y*-component.

Figure 2 shows two distance matrices produced by our DTW algorithm when comparing two walking motions. In dark areas the motions are equal, in

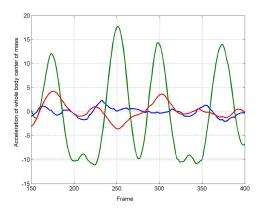


Figure 1: Accelerations of the center of mass of the entire body of a dancing motion involving different jumps. One can see two long non-contact phases corresponding to two long jumps and one short intermediate non-contact step (extract from motion 05\_16 from CMU mocap data base.)

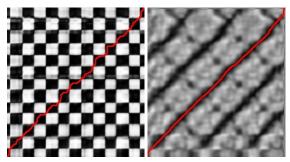


Figure 2: DTW distance matrices calculated on the base of different features. Acceleration of the whole body center of mass (left), acceleration of the whole body center of mass, hands and feet (right). The best warping paths are drawn red.

brighter areas the motions are unequal, corresponding to the given features. The red line is the warping path found by the algorithm. The left one is based only on the acceleration of the center of mass. In this checkerboard-like pattern we have thirteen black diagonals. This shows that we can not differentiate between the steps. If we add the acceleration of the feet to our features, the result gets obviously better. This can be seen in the right picture of figure 2. There we have got five dark diagonals, so steps made with the same foot are detected as similar.

The right matrix is not as symmetric as the left one. This shows that the motion is not similar to the same backward motion.

Depending on the motions that should be time warped, one can select specific features.

For walking motions the movement of the legs gives the most important features, if the steps should

be synchronized. For Karate-like kicking motions the foot that makes the kick is most important. The moments, in the compared motions, where the leg is stretched have to be matched to each other. Therefore features from this leg should get a higher weight. Another example we tested are cartwheel motions. To get a good correspondence for these motions, features that describe the motion of hands an feet are useful. A result of this warping technique for a walking motion is presented in the video.

## 4 RESULTS

For our experiments we built our motion model for three motion classes: walking, grabbing and cartwheel motions. For all of these motion classes we constructed data tensors with motion representation based on Euler angles and based on quaternions. Initially some preprocessing was required, consisting mainly of the following steps. All motions were

- a) filtered in the quaternion domain with a smoothing filter described in (Lee and Shin, 2002);
- b) aligned over time by the time warping using physics-based distance features;
- c) moved to the origin with their root node and oriented to the same direction;
- d) finally sampled down to a frame-rate of 30 Hz.

By applying the N-Mode SVD on the data tensors that were constructed of these motions we got the core-tensors  $\Phi$  that were used for the following experiments.

# 4.1 Walking Motions

For this motion class we used walking motions out of our database, from five actors which were asked to perform the following four motions for three times:

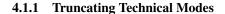
- walk four steps in a straight line.
- walk four steps in a half circle to the left side.
- walk four steps in a half circle to the right side.
- walk four steps on the place.

All motions had to start with the right foot. All motions were aligned over time to the length of the first motion of actor one. The five actors performing the motions all have been healthy young adult male persons.

All motions were repeated by all actors for three times. The actors were asked to stay within the same verbal description of the motion and its style, but nevertheless to have some variations in their interpretations of the motion and the style.

Table 1: Dimension, mean errors and size of the core tensor
for walking motions, represented by Euler angles.

Dimension	Mean error	Entries	
Core Tensor	walking motions	Core Tensor	
	(degrees)		
	ted Data Mode	201220	
$5022 \times 5 \times 4 \times 3$	0.0	301320	
$64 \times 5 \times 4 \times 3$	0.0	3840	
$61 \times 5 \times 4 \times 3$	0.0	3660	
$58 \times 5 \times 4 \times 3$	0.1	3480	
$55 \times 5 \times 4 \times 3$	0.3	3300	
$40 \times 5 \times 4 \times 3$	1.3	2400	
$25 \times 5 \times 4 \times 3$	2.6	1500	
$10 \times 5 \times 4 \times 3$	4.4	600	
$1 \times 5 \times 4 \times 3$	7.3	60	
Truncated DOF Mode			
$62 \times 81 \times 5 \times 4 \times 3$	0.0	301320	
$52 \times 81 \times 5 \times 4 \times 3$	0.0	252720	
$40 \times 81 \times 5 \times 4 \times 3$	0.2	194400	
$31 \times 81 \times 5 \times 4 \times 3$	0.8	150660	
$22 \times 81 \times 5 \times 4 \times 3$	1.5	106920	
$10 \times 81 \times 5 \times 4 \times 3$	3.8	48600	
$1 \times 81 \times 5 \times 4 \times 3$	11.2	4860	
Truncated Actor Mode			
$62 \times 81 \times 4 \times 4 \times 3$	3.1	241056	
$62 \times 81 \times 3 \times 4 \times 3$	5.2	180792	
$62 \times 81 \times 2 \times 4 \times 3$	6.8	120528	
$62 \times 81 \times 1 \times 4 \times 3$	9.4	60264	
Truncated Style Mode			
$62 \times 81 \times 5 \times 3 \times 3$	4.0	225990	
$62 \times 81 \times 5 \times 2 \times 3$	5.6	150660	
$62 \times 81 \times 5 \times 1 \times 3$	7.7	75330	
Truncated Repetition Mode			
$62 \times 81 \times 5 \times 4 \times 2$	2.1	200880	
$62 \times 81 \times 5 \times 4 \times 1$	4.7	100440	



For our truncation experiments we systematically truncated a growing number of components of the core-tensors and reconstructed all motions. The mean difference between all reconstructed and original motions – depending on the size of the truncated coretensor—is shown in table 1. The considered motions were warped to a length of 81 frames and our skeleton, based on Euler angles, has 62 degrees of freedom. On this basis the resulting data tensor has a size of  $5022 \times 5 \times 4 \times 3$ . The resulting core tensor after applying an N-Mode SVD was now reduced. In figure 3 the mean error E over all motions and all frames is shown graphically in dependence of the size of the Data Mode (blue). This error is defined as follows:

$$E = (\sum_{i}^{\text{Frames DOFS}} \sum_{j}^{\text{DOFS}} \text{abs}(e_{i,j}^{\text{org}} - e_{i,j}^{\text{rec}})) / (\text{Frames} \cdot \text{DOFS}),$$

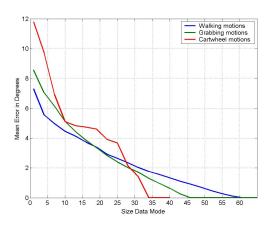


Figure 3: Mean error of reconstructed walking (blue), grabbing (green) and cartwheel (red) motions, depending on the size of the Data Mode of the core tensor.

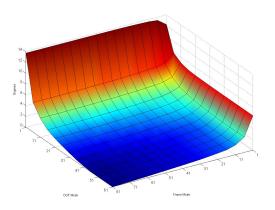


Figure 4: Displacement in degrees for truncated Frame and DOF Mode.

where Frames is the number of all frames of all motions that were used to build the data tensor, and DOFS is the number of degrees of freedom of the underlying skeleton. This error is always calculated on Euler angles hence the motions are stored in the ASF/AMC file format.

One can see that the motions are reconstructed without any visible error with no more than 61 of the original 5022 dimensions.

If the technical Data Mode is split up into the Frame and DOF Mode it is possible to make a similar experiment by truncating both modes. The result is shown in figure 4. If just the DOF Mode is truncated the motion is reconstructed with a mean error of less than one degree for more than 26 degrees of freedom. The same displacement can be reached by reducing the Frame Mode down to a size of 20.

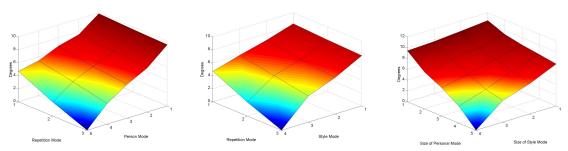


Figure 5: Mean error, in degrees, of reconstructed motions where two natural Modes were truncated. Style and Repetition Mode are truncated (left). Personal and Repetition Mode are truncated (middle). Style and Personal Mode are truncated (right).

# 4.1.2 Truncating Natural Modes

To verify the importance of natural modes we proceeded in the same way. In fact the displacement is at the lowest size for the Repetition Mode. This is what one would expect since the actors were asked to perform the same action multiple times. The reason for the observed displacement, is given through the different interpretations of the motions. Note that several interpretations from one actor are giving a smaller variance, than motions from different actors or motions in different styles. The results of these experiments are shown in figure 5. The displacement grows higher with the size of truncated values from Style-and Personal Mode.

# 4.2 Grabbing Motions

For this motion class the actors, which have been the same as for the walking motions, were asked to perform grabbing motions from a storage rack. The Style Mode is derived from three different heights (low, middle, and high). We took three takes of all motions, that the repetition-mode has a size of three. All grabbing motions were performed with the right hand. Again all motions were warped to the length of one reference motion. The data tensor has a size of  $f \cdot \text{dof} \times 5 \times 3 \times 3$ . The resulting error for truncated components of the Data Mode is shown in figure 3 (green).

# 4.3 Cartwheel Motions

The last class of motions we considered are cartwheel motions. We captured several cartwheels from four persons. All actors were asked to start their cartwheels with the left foot and the left hand. We did not define different "styles" for cartwheel motions. The core tensor had a size of  $6138 \times 4 \times 1 \times 3$ . Here

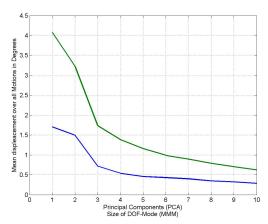
Table 2: Dimension, mean errors and size of the core tensor for grabbing motions, represented with Euler angles.

Dimension Core Tensor	Mean error grabbing motions (degrees)	Entries Core Tensor		
Trunca	ted Data Mode			
$4340 \times 5 \times 3 \times 3$	0.0	195300		
$58 \times 5 \times 3 \times 3$	0.0	2610		
$55 \times 5 \times 3 \times 3$	0.0	2475		
$40 \times 5 \times 3 \times 3$	0.6	1800		
$25 \times 5 \times 3 \times 3$	2.4	1500		
$10 \times 5 \times 3 \times 3$	5.1	450		
$1 \times 5 \times 3 \times 3$	8.6	45		
Truncated DOF Mode				
$62 \times 70 \times 5 \times 3 \times 3$	0.0	195300		
$52 \times 70 \times 5 \times 3 \times 3$	0.0	163800		
$40 \times 70 \times 5 \times 3 \times 3$	0.3	126000		
$31 \times 70 \times 5 \times 3 \times 3$	0.9	97650		
$22 \times 70 \times 5 \times 3 \times 3$	1.9	69300		
$10 \times 70 \times 5 \times 3 \times 3$	4.4	31500		
$1 \times 70 \times 5 \times 3 \times 3$	9.7	3150		

all motions could be reconstructed without any visible error for a size of no more than 34 for the Data Mode. This results are shown in table 4.3 and can be seen graphically in figure 3 (red).

#### 4.4 Comparison with PCA

To compare our multi-linear model with linear models, as they are used for principal component analysis (PCA), we constructed two tensors for our model and two matrices for the PCA based on the same motions. Figure 6 shows a comparison of the results for walking (left) and grabbing motions (right). The mean error over all reconstructed motions depending on the number of principal components and the size of the DOF Mode is shown in this figure. The mean error for motions reconstructed from the multi-mode-model is



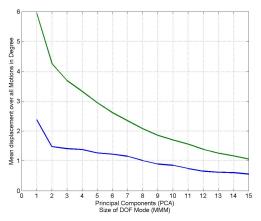


Figure 6: Mean error of reconstructed motions with reconstructions based on our model (blue) and based on a PCA (green). The result is shown for walking motions (left) and grabbing motions (right).

Table 3: Dimension, mean errors and size of the core tensor for cartwheel motions, represented by Euler angles.

Dimension Core Tensor	Mean error cartwheel motions (degrees)	Entries Core Tensor	
Truncated Data Mode			
$6138 \times 4 \times 1 \times 3$	0.0	73656	
$34 \times 4 \times 1 \times 3$	0.0	408	
$31 \times 4 \times 1 \times 3$	1.4	372	
$16 \times 4 \times 1 \times 3$	4.4	192	
$1 \times 4 \times 1 \times 3$	11.8	12	

smaller than the error from the motions reconstructed from principal components. Thus a motion can be reconstructed with a mean error less than one degree above the complete motion from a core tensor when the DOF Mode is truncated to just three components.

Thus especially in cases when a motion should be approximated by rather few components the reduction based on the multi-linear model is considerably better than the one done by PCA.

# 4.5 Motion Synthesis

As it was described in Sect. 2.4, it is possible to synthesize motions with our multi-linear model. For every mode i there is an appropriate matrix  $U_i$ , where every row  $u_{i,j}$  represents one of the motions j, this mode consists of. Therefore an inter- or extrapolation can be done between any rows of U before they are multiplied with the core tensor  $\Phi$  to synthesize a motion. To prevent our results from unrequested effects like turns and unexpected flips resulting from a repre-

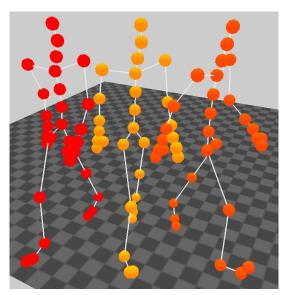


Figure 7: Screenshot from the original motions that are from the styles walking forward (red) and walking a left circle (orange), the synthetic motion (yellow) is produced by a linear combination of these styles.

sentation based on Euler angles we used our quaternion based representation to synthesize motions.

For the following walking example we constructed a motion that was interpolated between two different styles. The first style was walking four steps straight forward and the second one was walking four steps on a left round. We made a linear interpolation by multiplying the corresponding rows with the factor 0.5. The result is a four step walking motion that describes a left round, with a larger radius. One sample frame of this experiment can be seen in figure 7. Another synthetic motion was made by an interpolation

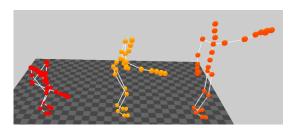


Figure 8: Screenshot from the original motions that are from the styles grabbing low (red) and grabbing high (orange), the synthetic motion (yellow) is produced by a linear combination of these styles.

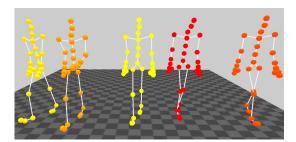


Figure 9: Screenshot from four original walking motions and one synthetic motion, that is an result of combining two, the personal and the style mode. The original motions of the first actor are on the left side, the original motions of the second actor are on the right side and the synthetic example can be seen in the middle.

of grabbing styles. We synthesized a motion by an interpolation of the styles grabbing low and grabbing high. The result is a motion that grabs in the middle. One result of this synthetic motion is shown in figure 8.

With this technique we are able to make interpolation between all modes parallel. One example is a walking motion that is an interpolation between the style and actors Mode. One picture of this result is given in figure 9.

For more detailed results of our motion synthesis we refer to the video.

# 5 CONCLUSION AND FUTURE WORK

We have shown that exploring naturally occurring modes in motion databases and representing motions in multi-linear models—after appropriate preprocessing—is a feasible way to represent motions of a database allowing different synthesis, analysis and compression of the motions. We expect that multi-mode representations will be either an interesting alternative or an additional toolkit in basically all

cases, in which currently principal component analysis is used. As has been shown by our experiments, the benefit of the multi-linear representation over a simply linear representation of a suitably structured collection of motion data is especially relevant if motions should be approximated by rather few components, e.g. in the context of reconstruction of motion by low-dimensional control signals (Chai and Hodgins, 2005) or in the context of auditory presentation of a motion (Droumeva and Wakkary, 2006; Röber and Masuch, 2005; Effenberg et al., 2005). This paper presents a proof of concept, for which we could use a motion database having examples for all data of the built tensors. In general one might only have sparsely given data for the different modes. However, we presume that techniques similar to the ones used to fill the data tensors in the case of faces from sparse data (Vlasic et al., 2005) can be used for motion data, too. It will be a topic of our future research to investigate these techniques and to apply the multi-mode representation to some of the tasks mentioned above.

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